

UNIT 24 Solving Quadratic Equations Introduction to SIM

Learning objectives

This unit is focused on methods of solving quadratic equations. After completing this unit of STUDENT INSTRUCTIONAL MATERIAL (SIM) you should

- be able to solve quadratic equations that factorise into two linear terms
- be able to use the formula for solving quadratic equations
- understand how to complete the square for a quadratic and hence solve the equation.

Key points and principles

- There are three methods of solving quadratic equations:

- (i) **quadratic factorisation**, where we can write

$$ax^2 + bx + c = a(x - p)(x - q) \text{ when } p \text{ and } q \text{ are rational numbers}$$

which has solution $x = p$ or $x = q$

- (ii) **formula**
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

- (iii) **completing the square**, where we write

$$ax^2 + bx + c = a\left(x + \frac{b}{2a}\right)^2 - \frac{b^2}{4a} + c$$

- Note that if $(x - a)(x - b) = 0$, then either $x - a = 0$ or $x - b = 0$, giving $x = a$ or $x = b$.
- Quadratic equations have 2, 1 or 0 real roots according to the value of " $b^2 - 4ac$ ":
 - (i) If $b^2 > 4ac$, there are 2 real distinct roots
 - (ii) If $b^2 = 4ac$, there is 1 (repeated) real root
 - (iii) If $b^2 < 4ac$, there are no real roots.

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Facts to remember

- If $(x - a)(x - b) = 0$ then $x = a$ or $x = b$

- The formula for solving the quadratic equation

$$ax^2 + bx + c = 0$$

is

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

- The number of real roots of a quadratic is

$$2 \text{ if } b^2 > 4ac$$

$$1 \text{ if } b^2 = 4ac$$

$$0 \text{ if } b^2 < 4ac$$

Glossary of Terms

Quadratic factorisation

This is when you can write a quadratic formula in the form

$$ax^2 + bx + c = a(x - p)(x - q)$$

Formula for solving quadratic equation

The formula for solving the quadratic equation

$$ax^2 + bx + c = 0$$

is

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Completing the square

This is when we write the quadratic in the form

$$ax^2 + bx + c = a\left(x + \frac{b}{2a}\right)^2 - \frac{b^2}{4a} + c$$